

## Generalized Doppler Effect

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Let  $S \equiv OXYZ$  and  $s \equiv oxyz$  be inertial frames in standard configuration, and assume that  $s$  translates parallel to  $OX$  with a constant velocity  $u$  ( $u > 0$ ). Let  $b$  be a source of light that is stationary in  $s$ , and hence moving with a constant velocity  $u$  relative to  $S$ . Suppose that the source  $b$  is radiating a monochromatic light of wavelength  $\lambda$ . This will be received by  $o$  as monochromatic light of the same wavelength. Let  $(R, \theta, \varphi)$  and  $((r, \theta, \varphi)$  be the spherical coordinates of the source  $b$  in  $S$  and  $s$  respectively.

The moment at which light first reaches the contiguous observers  $o$  and  $O$  corresponds to  $r = ct$ . Setting  $r = ct$  in the generalized Lorentz transformations [1] yields

$$(1) \quad R = \gamma (\sqrt{1 - \beta^2 \sin^2 \theta} r + \beta \cos \theta)$$

Now assume that the distance  $r$  in the moving frame corresponds to one wave-length, i.e.  $r = \lambda$ . With respect to the observer  $O$  the distance  $R$  corresponds to one wave-length  $\lambda'$ .

### Generalized Doppler's formula

Substituting in the last equation  $r = \lambda$  and  $R = \lambda'$ , we obtain:

$$(2) \quad \lambda' = \gamma (\sqrt{1 - \beta^2 \sin^2 \theta} + \beta \cos \theta) \lambda,$$

with  $\gamma = 1 / \sqrt{1 - \beta^2}$ , which determines the wave length as measured by the stationary observer. Note that the radiating source here is at a position of azimuth angle  $\theta$ , and that the polar axis is  $OX$ .

### Longitudinal Doppler's Formula

Setting  $\theta = 0$  in the generalized formula (1) we obtain

$$(3) \quad \lambda' = \sqrt{\frac{1 + \beta}{1 - \beta}} \lambda$$

which is the red shift Doppler's formula, corresponding to the source and the observer receding from each other. For  $\theta = \pi$  we obtain the blue shift Doppler's formula

$$(4) \quad \lambda' = \sqrt{\frac{1-\beta}{1+\beta}} \lambda$$

corresponding to the source and the observer approaching each other.

### **Transpose Doppler's Effect**

Setting  $\theta = \pi/2$  in (2) we find

$$(5) \quad \lambda' = \lambda.$$

Hence, and contrary to the relativistic prediction, there is no transpose Doppler's effect.

### **References**

[1] C P Viazminsky, Generalized Lorentz transformations and Restrictions on Lorentz Transformation, Research Journal of Aleppo University, 48, 2007.